# ISAACS: Iterative Soft Adversarial Actor-Critic for Safety

Kai-Chieh Hsu\*, Duy Phuong Nguyen\*, Jaime F. Fisac









# Scalable Safety Analysis in Robotics

Rigorous robust optimal control tools scale poorly to high-dimensional nonlinear dynamics.

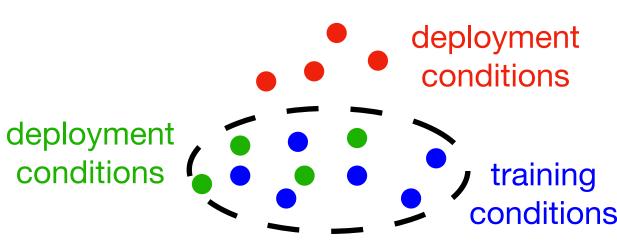
Computation time and memory (logarithmic scale)

Limit of numerical tractability (finite-element dynamic programming)

5 10 15 20 25 30 35 40

Number of continuous state dimensions

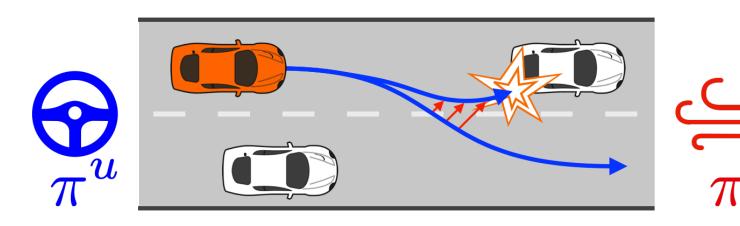
Scalable deep learning methods lack guarantees and are brittle to "out-of-distribution" conditions.



Can we devise computational safety tools for uncertain, high-dimensional dynamical systems without renouncing strict safety guarantees?

# Offline Safety Synthesis (ISAACS)

1. State-action sequences collected by a series of simulated adversarial safety games



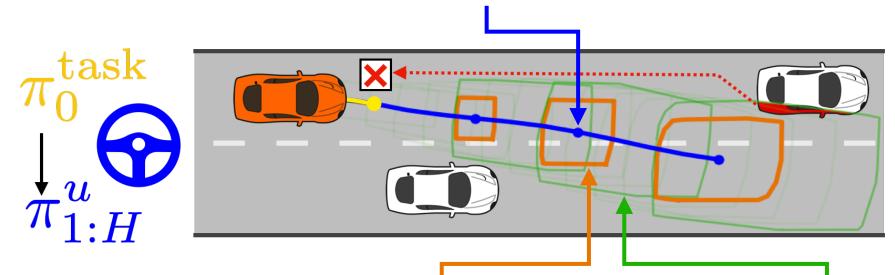
2. Controller/disturbance policies (actors) & safety value (critic) co-trained via safety Isaacs equation:

$$V(x) = (1 - \gamma)g(x) + \gamma \max_{\pi_u} \min_{\pi_d} \mathbb{E}\min_{u,d} \left\{ g(x), Q(x,u,d) \right\}$$

3. Leaderboard update via *cross-play*: rank policy versions by win rate vs. all opponents, keep top *k* 

#### Online Safety Certification

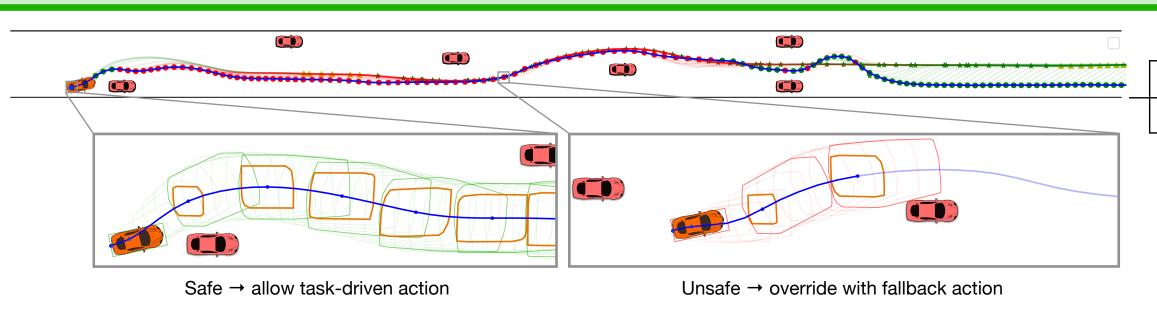
1. Reference fallback trajectory by rolling out the untrusted ISAACS policy after 1 task-driven action

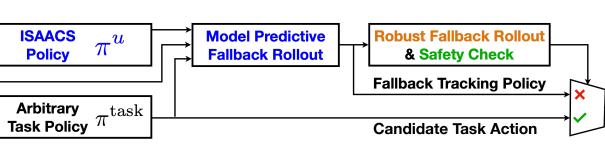


2. Robust fallback rollout through forward-reachable sets (tracking bounds)

3. Certification by checking *footprint-augmented* forward-reachable sets for collisions/violations

# Safety Filter

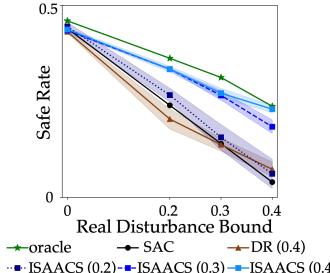


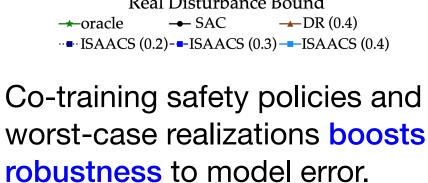


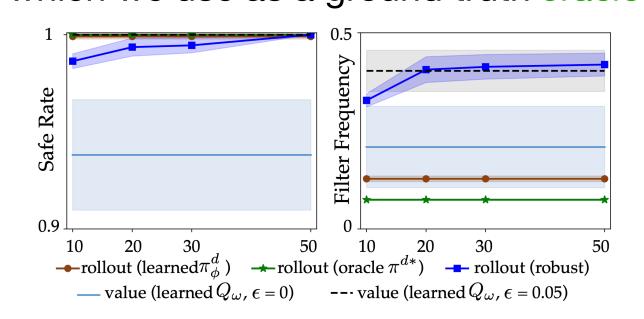
At each time, the task policy's control is allowed *if* it leaves open the option to track the fallback policy *later* and still maintain safety under all uncertainty realizations.

# Evaluation: autonomous car

We validate ISAACS on a 5D car system, at the computability limit of "exact" numerical solutions, which we use as a ground truth *oracle*.



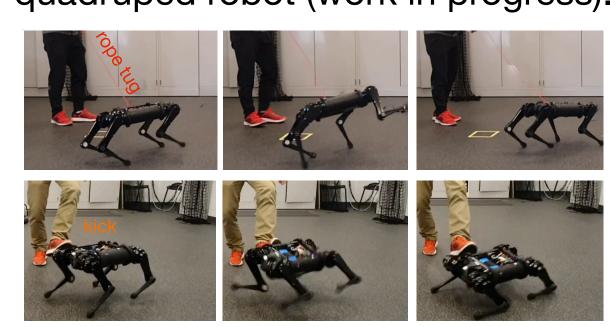




The ISAACS robust rollout safety filter achieves a perfect 100% safe rate (0 violations). The direct gameplay rollout/value filters can fail, but rarely do!

# Sneak peek: quadruped

We are testing ISAACS on a 36D quadruped robot (work in progress).



The ISAACS safety policy, learned purely in simulation and deployed with a value filter, responds to various attacks to prevent falls.